

## EPR, optical absorption and superposition model study of Fe<sup>3+</sup> doped strontium nitrate single crystals

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### ABSTRACT

Electron paramagnetic resonance (EPR) study of Fe<sup>3+</sup> ions doped strontium nitrate (SN) single crystals is performed at liquid nitrogen temperature and at X band frequency. The spin Hamiltonian (SH) parameters are determined from the resonance lines observed at different angular rotations. The crystal field parameters (CFPs) are evaluated using superposition model of Newman. The Zeeman g-factor and zero-field splitting parameters (ZFSPs) of Fe<sup>3+</sup> ion in SN (truncated SH considered) are:  $g = 1.9989 \pm 0.002$  and  $|D| = (338 \pm 5) \times 10^{-4} \text{ cm}^{-1}$ ,  $|E| = (10 \pm 5) \times 10^{-4} \text{ cm}^{-1}$ ,  $a = (458 \pm 5) \times 10^{-4} \text{ cm}^{-1}$ , respectively. The Fe<sup>3+</sup> ion enters the lattice substitutionally replacing the Sr<sup>2+</sup> sites of cubic symmetry. The local site symmetry of Fe<sup>3+</sup> ion in the crystal is orthorhombic (lower than that of the host). The optical absorption study of the crystal is also done at room temperature in the wavelength range 195–925 nm. The energy values of different orbital levels are determined. The observed bands are assigned as transitions from the <sup>6</sup>A<sub>1g</sub>(S) ground state to various excited states of Fe<sup>3+</sup> ion in a cubic crystal field approximation. The observed band positions are fitted with four parameters, the Racah interelectronic repulsion parameters (B and C), the cubic crystal field splitting parameter (Dq) and the Trees correction ( $\alpha$ ) yielding:  $B = 934$ ,  $C = 2059$ ,  $Dq = 1450$ , and  $\alpha = 90$  (in cm<sup>-1</sup>). On the basis of EPR and optical data, the nature of metal–ligand bonding in this crystal is discussed. The ZFSPs are also determined theoretically using microscopic SH theory based on perturbation theory and CFPs,  $B_{kq}$  obtained from superposition model. The values of ZFSPs thus obtained are  $|D| = (340 \pm 5) \times 10^{-4} \text{ cm}^{-1}$  and  $|E| = (15 \pm 5) \times 10^{-4} \text{ cm}^{-1}$ .

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### 1. Introduction

Electron paramagnetic resonance (EPR) study provides information about the local site symmetry and zero-field splitting (ZFS) parameters of transition ions in crystals [1,2]. It is also used to identify the defects responsible for the charge compensation in impurity doped crystals [3]. The optical absorption study is used to find the crystal field strength and the energy level structure of the doped ion [4]. Thus EPR and optical absorption are two supplementary powerful tools to investigate the local environment around the transition ion doped into various crystals, because both of them are very sensitive to distortion of the local lattice structure of the impurity ion. Transition ion doped crystals are important due to their spectroscopic properties making them suitable for laser and optical fiber applications. In the iron group, Fe<sup>3+</sup> ion is of interest because the 3d<sup>5</sup> shell, responsible for paramagnetism, is just half filled yielding the resultant angular momentum to be zero in the ground state <sup>6</sup>S with spin  $S = 5/2$ . The crystalline electric field

can affect the electron spins only through high-order interactions, so that the spins are almost completely free to orient themselves in an external magnetic field.

Strontium nitrate, Sr(NO<sub>3</sub>)<sub>2</sub>(SN) is a white granular compound which is used as a precursor for the production of high-purity compounds [5], nanotechnology powders and suspensions [6]. SN is most commonly used in pyrotechnics for the production of red colour, signal lights, marine signals and railroadflares [7]. Due to such applications, the growth and characterization of SN is important.

In the present investigation, the EPR and optical absorption of Fe<sup>3+</sup> ion in SN are carried out at liquid nitrogen (77 K) and room temperature (300 K), respectively. The purpose of study is to obtain information whether Fe<sup>3+</sup> ion enters the lattice substitutionally or interstitially, to predict the distortion in the lattice, to find energy separations between different orbital levels, and to describe the nature of bonding of Fe<sup>3+</sup> ion with its various ligands in the crystal. Theoretical investigations of ZFS parameters are also performed using perturbation theory and crystal field parameters obtained from superposition model [8]. The theoretical results obtained using superposition model are found to be in agreement with the experimental results.

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## 2. Crystal structure

SN single crystals are cubic with space group  $Pa\bar{3}$ . The unit cell parameters are  $a = b = c = 0.78220$  nm with  $Z = 4$  [9,10]. The  $\text{Sr}^{2+}$  ions form a cubic face centered lattice. They are 12-coordinated by O-atoms, six at a distance of 0.27305 nm and the other six at a distance of 0.28492 nm. The N atoms are located on a threefold rotation axis. They are bonded to three O atoms with a distance of 0.12609 nm. The environment of nitrate group in SN is shown in Fig. 1. The  $\text{Sr}^{2+}$  sites have cubic symmetry.

## 3. Experimental

SN single crystals were grown at room temperature by slow evaporation of aqueous solution of strontium nitrate. For  $\text{Fe}^{3+}$  doped crystals 0.01 mol%  $\text{Fe}_2(\text{SO}_4)_3$  was added to the aqueous solution. Good colourless crystals of  $\text{Fe}^{3+}:\text{SN}$  were obtained in about 15–20 days. The EPR spectra of the crystals so prepared were recorded at 77 K on Varian X-band E-112 (9.1 GHz) reflection type spectrometer with 100 kHz field modulation. The single crystal was mounted at the end of a quartz-rod using wax and then aligned in  $\text{TE}_{102}$  cavity center to avoid RF field deterioration. The spectra were recorded as the first derivative of EPR absorption along the three mutually perpendicular crystallographic axes  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$  by rotating the crystal at every  $10^\circ$  using a goniometer.

The optical absorption spectra of  $\text{Fe}^{3+}$  ion doped SN crystals were recorded on a UNICAM – 5625 – UV/Visible spectrophotometer in the wavelength range 195–925 nm at room temperature.

## 4. Results and discussion

The recorded EPR spectra for  $\text{Fe}^{3+}:\text{SN}$  crystals at liquid nitrogen temperature when the applied magnetic field  $\mathbf{B}$  is parallel to the ' $\mathbf{a}$ ' axis is shown in Fig. 2. For  $\mathbf{B}$  in each of the three planes  $ab$ ,  $bc$  and  $ca$  a strong broad line is observed. This is assigned to the transition  $M = +1/2 \leftrightarrow -1/2$  [11]. In addition, two weak broad lines are also observed at two different orientations ( $0^\circ$  and  $90^\circ$ ) in the  $bc$  plane which are assigned to the transitions  $M = -3/2 \leftrightarrow -5/2$  and

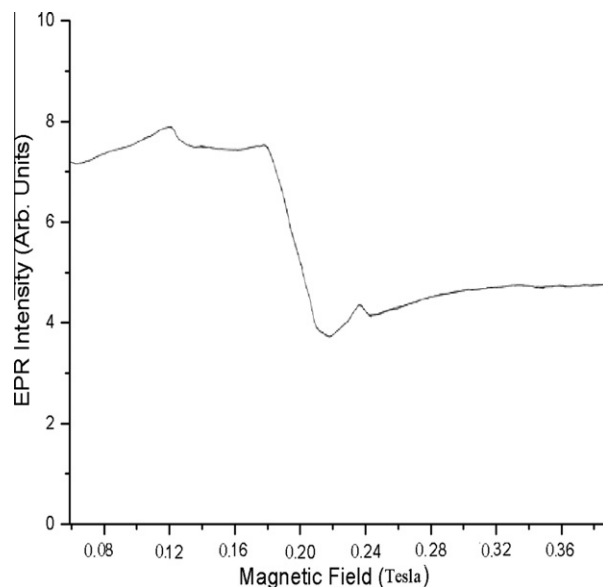


Fig. 2. EPR spectrum of  $\text{Fe}^{3+}$  ion doped SN single crystals with the magnetic field applied parallel to the  $\mathbf{a}$ -axis.

$M = -1/2 \leftrightarrow -3/2$ , respectively. No lines corresponding to other transitions were observed even when the magnetic field was scanned up to 0.6 T. The absence of fine structure lines corresponding to other transitions ( $M = 3/2 \leftrightarrow 1/2$  and  $M = 5/2 \leftrightarrow 3/2$ ) may be yielding larger linewidth similar to the case of  $\text{Fe}^{3+}$  in  $\text{BaTiO}_3$  [12] due to the internal strain. This may also be attributed to small axial ZFS term [13] (discussed later).

When  $\text{Fe}^{3+}$  ion is introduced in SN crystal, it can substitute for  $\text{Sr}^{2+}$  ions and local site symmetry is reduced to rhombic (lower than that of the host) as is observed in EPR spectra. By the combined effect of crystal field and magnetic interactions [14], the splitting of energy levels of  $\text{Fe}^{3+}$  ion takes place. The experimental resonance fields are analyzed using the spin Hamiltonian [11,15]

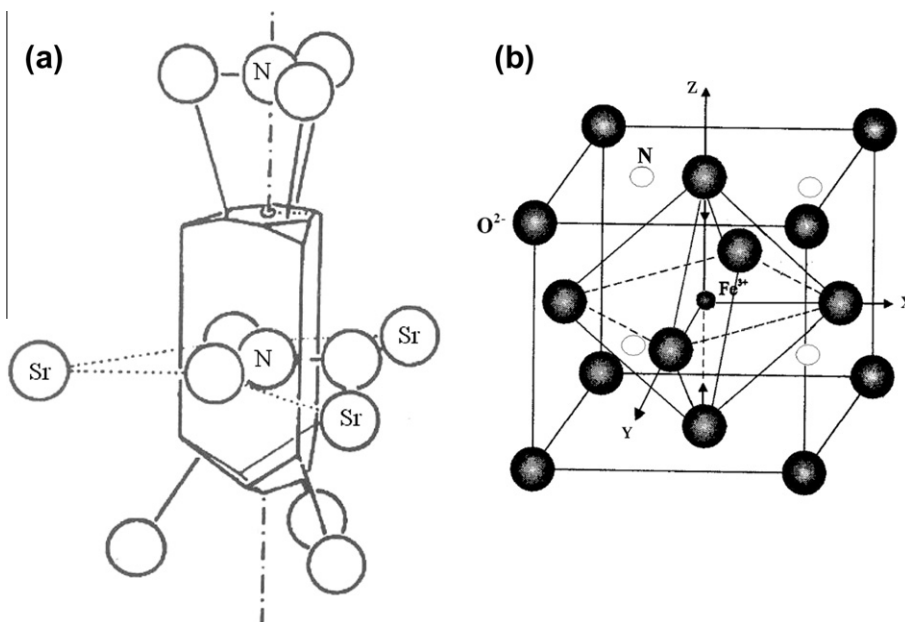


Fig. 1. (a) Environment of the nitrate groups in SN. Unmarked circles denote oxygen atoms (by the courtesy of Nowotny and Heger [8]). (b) Coordination around  $\text{Fe}^{3+}$  in SN.

$$\begin{aligned} \mathcal{H} = & g\mu_B \mathbf{B} \cdot \mathbf{S} + D \left\{ S_z^2 - \frac{1}{3} S(S+1) \right\} + E (S_x^2 - S_y^2) \\ & + \left( \frac{a}{6} \right) \left[ S_x^4 + S_y^4 + S_z^4 - \frac{1}{5} S(S+1)(3S^2 + 3S - 1) \right] + \frac{F}{180} \\ & \times \{ 35S_z^4 - 30S(S+1)S_z^2 + 25S_z^2 - 6S(S+1) + 3S^2(S+1)^2 \} \\ & + \frac{K}{4} \left[ \{ 7S_z^2 - S(S+1) - 5 \} (S_+^2 + S_-^2) + (S_+^2 + S_-^2) \{ 7S_z^2 - S(S+1) - 5 \} \right] \\ & + AS_zI_z + B(S_xI_x + S_yI_y) \end{aligned} \quad (1)$$

where  $g$  is the isotropic spectroscopic splitting factor;  $\mu_B$ , the Bohr magneton;  $\mathbf{B}$ , the external magnetic field. The parameters  $D$  and  $E$  are the second-rank axial and rhombic ZFS parameters, whereas  $a$ ,  $F$ , and  $K$  are the fourth-rank cubic, axial and rhombic ones, respectively. The last two terms in Eq. (1) represent the hyperfine ( $I = 5/2$ ) interaction. The  $F$  and  $K$  ZFS terms are omitted here as their effect is small [11,16,17]. The isotropic approximation used for the electronic Zeeman interaction is generally valid for  $3d^5$  ions [1,11]. The two approximations in question may slightly affect the fitted value of  $a$  [18]. The direction of the maximum overall splitting of EPR spectrum is taken as the  $z$  axis and that of the minimum as the  $x$  axis [19]. The laboratory axes ( $x, y, z$ ) determined from EPR spectra are found to coincide with the crystallographic axes (CA). The  $Z$ -axis of the local site symmetry axes, i.e. the symmetry adapted axes (SAA), is along the metal oxygen bond Sr(1)–O(4) bond in the crystal and the other two axes ( $X, Y$ ) are perpendicular to the  $Z$ -axis (Fig. 1). The allowed transitions and the corresponding resonance fields  $B$  for the case of dominant Zeeman interaction are given [11,20] by the equations in Appendix A.

Fig. 3 shows the angular variation of the EPR resonance line,  $M = +1/2 \leftrightarrow -1/2$ . The values of spin Hamiltonian parameter  $g$ ,  $|D|$ ,  $|E|$  and  $a$  obtained using self developed computer program are given in Table 1. The  $\mathbf{g}$  tensor is calculated at different orientations in all the three planes and then diagonalised using the procedure of Schonland [21] to obtain the principal values:  $g_x$ ,  $g_y$  and  $g_z$ .  $\mathbf{D}$  tensor is calculated by fitting Eq. (A.3) for the transition  $M = +1/2 \leftrightarrow -1/2$  to the experimental resonance fields in all three planes  $ab$ ,  $bc$  and  $ca$ . The values of  $\mathbf{D}$  obtained in  $ab$ ,  $bc$  and  $ca$  planes are considered to correspond to  $D_z$ ,  $D_x$  and  $D_y$ , respectively. Then  $D$  and  $E$  can be determined by the method given in [15], whereas  $a$  is calculated by fitting Eqs. (A.4) and (A.5) for the transitions  $M = -1/2 \leftrightarrow -3/2$  and  $M = -3/2 \leftrightarrow -5/2$  to the observed resonance fields at two different orientations ( $0^\circ$  and  $90^\circ$ ) in the  $bc$  plane. The directions of the principal axes of the  $\mathbf{D}$  tensor are nearly the same as that of the  $\mathbf{g}$  tensor. From Table 1, it is seen that  $|D|$  is smaller

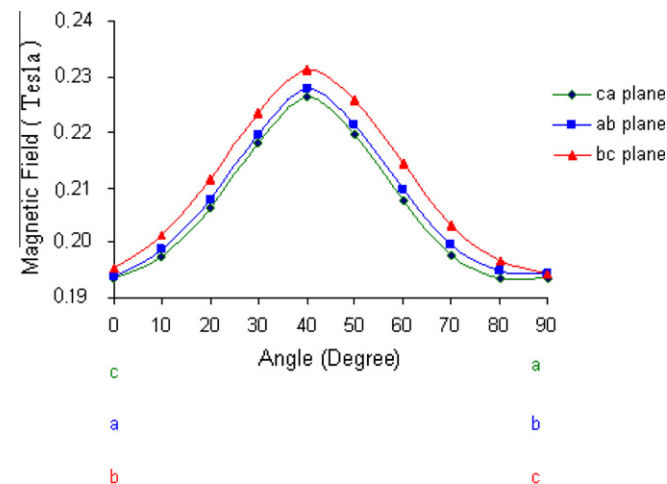


Fig. 3. Angular variation of the EPR spectrum of  $\text{Fe}^{3+}:\text{SN}$  in three planes  $ca$ ,  $ab$  and  $bc$  (solid lines represent theoretical plot and symbols are experimental points).  $ca$  ( $c$  at  $0^\circ$ ,  $a$  at  $90^\circ$ );  $ab$  ( $a$  at  $0^\circ$ ,  $b$  at  $90^\circ$ );  $bc$  ( $b$  at  $0^\circ$ ,  $c$  at  $90^\circ$ ).

Table 1

Experimental spin Hamiltonian parameters  $g$  and  $D$ ,  $E$ ,  $a$  (in  $10^{-4} \text{ cm}^{-1}$ ) for  $\text{Fe}^{3+}$  ion in SN together with  $\text{Fe}^{3+}$  in  $\text{BaTiO}_3$  single crystals and comparison of theoretical and experimental ZFS parameters for  $\text{Fe}^{3+}:\text{SN}$ .

System	$g$	$ D $	$ E $	$a$
$\text{Fe}^{3+}:\text{BaTiO}_3$	$g = 2.003$	23	113	113
	$g_x = 1.936$	$D_x = 200$	338	458
$\text{Fe}^{3+}:\text{SN}$	$g_y = 2.002$	$D_y = 220$	10	
	$g_z = 2.058$	$D_z = 225$		
Theoretical		340	15	

$$g = (g_x + g_y + g_z)/3 = 1.999.$$

Estimated errors for  $g$ ,  $D$  and  $a$  values are  $\pm 0.002$  and  $\pm 5 \times 10^{-4} \text{ cm}^{-1}$ , respectively.

<sup>a</sup> Present study.

than  $a$  (similar to  $\text{Fe}^{3+}:\text{BaTiO}_3$  [12], Table 1) and thus this may be the expected reason of absence of some fine structure lines as mentioned earlier.

To find out whether  $\text{Fe}^{3+}$  ion enters the SN lattice substitutionally or interstitially, the direction cosines of different bonds are calculated from the crystal structure data (Table 2) and compared with the direction cosines of  $\mathbf{g}$  obtained from EPR study. The direction cosines of Sr(1)–O(4) bond agree reasonably well with those for the experimental  $g_z$ . This indicates that  $\text{Fe}^{3+}$  ion substitutes at  $\text{Sr}^{2+}$  site (Fig. 1). Also the ionic radius of  $\text{Fe}^{3+}$  ion (0.064 nm) [14] is smaller than that of  $\text{Sr}^{2+}$  ion (0.112 nm) [22]. Thus,  $\text{Fe}^{3+}$  ion can fit well at the place of  $\text{Sr}^{2+}$  ion.

This is consistent with the conclusion drawn on the basis of direction cosines. The charge compensation in the crystal is effected either by excess oxygen ions [23] or by vacancies distributed at random throughout the crystal.

## 5. Optical absorption study

The recorded optical spectra of  $\text{Fe}^{3+}$  doped SN single crystals at room temperature are given in Fig. 4. The optical spectra consist of 18 bands located at 10916, 11650, 12024, 13793, 14888, 16173, 17839, 18576, 19544, 21403, 22472, 23904, 26746, 32796, 35455, 37412, 39948, and 40789  $\text{cm}^{-1}$ . Under cubic site symmetry approximation, the ground state term of  $\text{Fe}^{3+}$  ion is  ${}^6A_{1g}(S)$ . The first four excited multiplets are  ${}^4G$ ,  ${}^4P$ ,  ${}^4D$ , and  ${}^4F$ . The shortest wavelength band at 10916  $\text{cm}^{-1}$  may be considered due to infrared overtone and/or combination bands (the sum of two or more different wave numbers) [24]. The bands at 11650, 12024 and 13793  $\text{cm}^{-1}$  may be the split components of  ${}^6A_{1g}(S) \rightarrow {}^4T_{1g}(G)$  transition [25]. The bands at 14888, 16173, 17839, 18576 and 19544  $\text{cm}^{-1}$  are split components of  ${}^6A_{1g}(S) \rightarrow {}^4T_{2g}(G)$  [25]. The sharp bands at 21403 and 26746  $\text{cm}^{-1}$  are assigned to  ${}^6A_{1g}(S) \rightarrow {}^4E_g(G)$  and  ${}^6A_{1g}(S) \rightarrow {}^4E_g(D)$  transitions, respectively [25]. The bands at 22472, 23904, 32796 and 35455  $\text{cm}^{-1}$  are due to  ${}^6A_{1g}(S) \rightarrow {}^4A_{1g}(G)$ ,  ${}^6A_{1g}(S) \rightarrow {}^4T_{2g}(D)$ ,  ${}^6A_{1g}(S) \rightarrow {}^4T_{1g}(P)$  and  ${}^6A_{1g}(S) \rightarrow {}^4A_{2g}(F)$  transitions. The bands at 37412, 39948 and 40789  $\text{cm}^{-1}$  may be split components of  ${}^6A_{1g}(S) \rightarrow {}^4T_{1g}(F)$  transition. The two higher wavelength bands corresponding to  ${}^6A_{1g}(S) \rightarrow {}^4A_{2g}(F)$  and  ${}^6A_{1g}(S) \rightarrow {}^4T_{1g}(F)$  transitions are assigned using the energy matrices given by Tanabe and Sugano [26]. The above assignments are consistent with earlier studies [25,26].

The energy levels are evaluated using the Racah parameters ( $B$  and  $C$ ), the cubic crystal field splitting parameter ( $Dq$ ) and the Trees correction ( $\alpha$ ). The correction term is relatively small, and so it is arbitrarily fixed at the free ion value of 90  $\text{cm}^{-1}$  [27,28]. The parameters  $B$ ,  $C$  and  $Dq$  are obtained using equations [29] given in Appendix B.

After assigning the bands,  $B$  and  $C$  are determined using Eqs. (B.1) and (B.2) and used in solving the secular equations [30] to

**Table 2**The ionic distances and direction cosines of different bonds for Fe<sup>3+</sup>:SN.

Bond	Ionic distances (Å)	Direction cosines with respect to crystallographic axes		
		a	b	c
Sr(1)–O(1)	4.830	±0.4421	±0.4596	±0.7703
Sr(1)–O(2)	2.731	±0.6193	±0.0698	±0.7821
Sr(1)–O(3)	2.849	±0.7792	±0.0669	±0.6232
<b>Sr(1)–O(4)</b>	<b>8.144</b>	<b>±0.2180</b>	<b>±0.2726</b>	<b>±0.9371</b>
Sr(1)–N(1)	4.661	±0.5774	±0.5774	±0.5774
Sr(1)–N(2)	3.197	±0.3817	±0.3817	±0.8418
Sr(1)–N(3)	3.197	±0.8418	±0.3817	±0.3817
Sr(1)–N(4)	7.233	±0.1687	±0.3720	±0.9128
[g]		<b>±0.0499</b>	<b>±0.9689</b>	<b>±0.2422</b>
		<b>±0.9599</b>	<b>±0.0204</b>	<b>±0.2795</b>
		<b>±0.2758</b>	<b>±0.2465</b>	<b>±0.9291</b>

evaluate  $Dq$ . The energy values for quartet electronic states have been calculated for different values of  $Dq$  with  $B = 934 \text{ cm}^{-1}$ ,  $C = 2059 \text{ cm}^{-1}$  and  $\alpha = 90 \text{ cm}^{-1}$ . A good match of the experimental band positions with the predicted ones is obtained for  $Dq = 1450 \text{ cm}^{-1}$  as shown in Fig. 5. The band positions and their assignments are given in Table 3. The observed and calculated values are in good agreement, justifying the assignments.

The considerable decrease in the value of the Racah parameters  $B$  and  $C$  (from 1130 (free ion [31]) to 934, and 4111 to 2059  $\text{cm}^{-1}$ ) reveals a strong covalent bonding between the central metal ion and the ligands. By analogy with the peak at 407 nm [25] due to Fe<sup>3+</sup> centre in yttrium aluminium garnet at an octahedral site, the band at 418 nm may be considered as for Fe<sup>3+</sup>:SN thus confirming Fe<sup>3+</sup> ion at an octahedral site in SN.

## 6. Theoretical investigation

In this section, the ZFS parameters (ZFSs) of Fe<sup>3+</sup> ion located at Sr<sup>2+</sup> site in SN are calculated using the microscopic spin Hamiltonian (MSH) theory [15,32]. The crystal-field theory has been extensively applied to the study of the spin Hamiltonian parameters of transition metal ions in crystals [14,33–35]. These works discuss different contributions to ZFSs and give formulae to determine ZFSs of the 3d<sup>*N*</sup> ions including d<sup>5</sup> ion in terms of the electrostatic, the spin–orbit coupling, and the crystal-field parameters.

For a transition ion in a crystal, the crystal field Hamiltonian can be written as [31].

$$\mathcal{H} = \sum_{k,q} B_{kq} C_q^{(k)} \quad (2)$$

where  $B_{kq}$  are the crystal-field parameters and  $C_q^{(k)}$  are the Wybourne spherical tensor operators. For the orthorhombic crystal field,  $B_{kq} \neq 0$  only with  $k = 2, 4, q = 0, 2, 4$ . Point-charge model and superposition model are generally used to calculate the crystal-field parameters [8,36]. In the present study, we have calculated the crystal-field parameters,  $B_{kq}$  using superposition model. This model has been satisfactorily employed for several 3d<sup>*n*</sup> ions [14,33–35].

For orthorhombic symmetry, the SO contributions to the ZFS parameters  $D$  and  $E$  of 3d<sup>5</sup> ions were derived [37]:

$$D^{(4)}(\text{SO}) = (3\xi^2/70P^2D)(-B_{20}^2 - 21\xi B_{20} + 2B_{22}^2) + (\xi^2/63P^2G)(-5B_{40}^2 - 4B_{42}^2 + 14B_{44}^2) \quad (3)$$

$$E^{(4)}(\text{SO}) = (\sqrt{6}\xi^2/70P^2D)(2B_{20} - 21\xi)B_{22} + (\xi^2/63P^2G)(3\sqrt{10}B_{40} + 2\sqrt{7}B_{44})B_{42} \quad (4)$$

where  $P = 7B + 7C$ ,  $G = 10B + 5C$ , and  $D = 17B + 5C$ ;  $B$  and  $C$  are the Racah parameters.

By considering the covalency effect via the average covalency parameter  $N$ , the  $B$ ,  $C$  and  $\xi$  can be expressed in terms of  $N$  as [31,38,39],

$$B = N^4 B_0, C = N^4 C_0; \xi_d = N^2 \xi_d^0 \quad (5)$$

where  $B_0$  and  $C_0$ , and  $\xi_d^0$  are the free ion Racah and the spin–orbit coupling parameters, respectively [31,39]. For Fe<sup>3+</sup> ion, the following values are used:

$$B_0 = 1130 \text{ cm}^{-1}, C_0 = 4111 \text{ cm}^{-1}, \xi_d^0 = 589 \text{ cm}^{-1} [31].$$

Using optical study (this work):  $B = 934 \text{ cm}^{-1}$  and  $C = 2059 \text{ cm}^{-1}$ . Eq. (5) yield  $N = 0.953$  and  $N = 0.841$ , respectively. The average value of  $N = 0.897$  is used to calculate the ZFS parameters  $D$  and  $E$  from Eqs. (3) and (4).

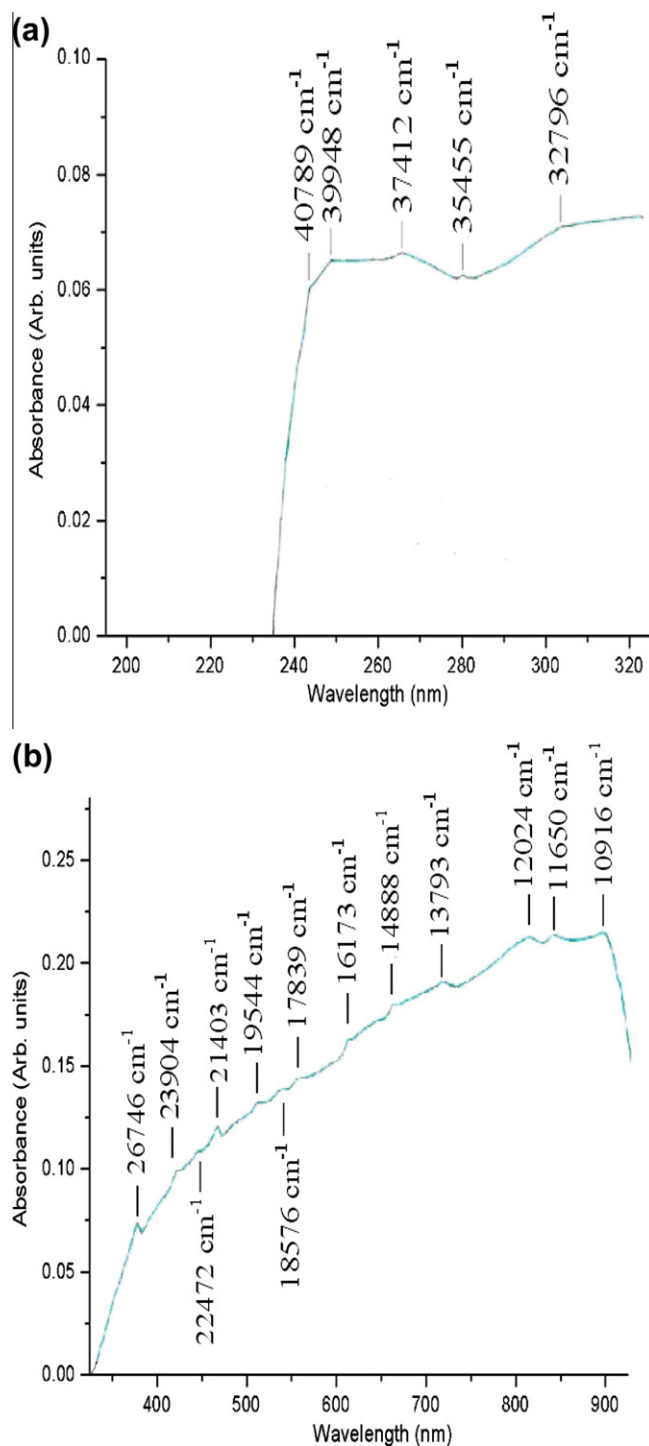
The superposition model expresses the  $B_{kq}$  parameters as [37,40]

$$B_{kq} = \sum \bar{A}_k(R_j) K_{kq}(\theta_j, \phi_j) \quad (6)$$

where  $R_j$  are the distances between the paramagnetic ion Fe<sup>3+</sup> and the ligand ion  $j$ ,  $R_0$  is the reference distance, normally chosen near a value of the  $R_j$ 's.  $\theta_j$  are the bond angles in a chosen axis system (preferably SAAS) [8,40]. Summation is taken over all the nearest neighbour ligands. The coordination factors  $K_{kq}(\theta_j, \phi_j)$  are the explicit functions of angular position of ligand [8,36,37]. The intrinsic parameter  $\bar{A}_k(R_j)$  is given by the power law [37], i.e.

$$\bar{A}_k(R_j) = \bar{A}_k(R_0)(R_0/R_j)^{t_k} \quad (7)$$

where  $\bar{A}_k(R_0)$  is the intrinsic parameter for a given ion host system;  $t_k$  is power law exponent. For Fe<sup>3+</sup>–O<sup>2-</sup> bonds,  $t_2 = 3$  and  $t_4 = 5$  [31]. For 3d<sup>5</sup> ions,  $\bar{A}_2(R_0)/\bar{A}_4(R_0)$  is 8–12 [41–43]. In the present study, we have taken  $\bar{A}_2(R_0)/\bar{A}_4(R_0) = 10$ , the middle value of 8 and 12. For 3d<sup>*N*</sup> ions in the 6-fold cubic coordination  $\bar{A}_4(R_0)$  can be found from the relation [44]:  $\bar{A}_4(R_0) = (3/4)Dq$ . As  $\bar{A}_4(R_0)$  is independent of the coordination [14], we have used above relation to determine  $\bar{A}_4(R_0)$  in our calculation. This gives  $\bar{A}_4(R_0) = 1087.5 \text{ cm}^{-1}$  and  $\bar{A}_2(R_0) = 10875 \text{ cm}^{-1}$ . The values of  $R_0, R_1, R'_1, R_2, R'_2; \theta_1, \theta'_1, \theta_2, \theta'_2; \phi_1, \phi'_1, \phi_2$  and  $\phi'_2$  used in the calculation are: 0.1620 nm [45], 0.2849 nm, 0.2849 nm, 0.4830 nm, 0.5935 nm; 90.489°, 94.569°, 84.349°, 97.035°; 51.349°, 4.906°, 46.108° and –6.428°, respectively. There may be considerable covalent bonding between Fe<sup>3+</sup>–O<sup>2-</sup>, and thus the reference distance (bond length)  $R_0$  could be smaller than the sum of the ionic radii  $r_{O^{2-}}$  (=0.132 nm) and  $r_{Fe^{3+}}$  (=0.064 nm). This is partially supported by the data on Ni<sup>3+</sup> substituting for K<sup>+</sup> in KTaO<sub>3</sub> [46] where  $R_0$  is about 0.176 nm which is 0.019 nm smaller than the sum of radii  $r_{O^{2-}}$  (=0.132 nm) and  $r_{Ni^{3+}}$  (=0.063 nm). Hence, in view of the above,  $R_0$  between Fe<sup>3+</sup> and O<sup>2-</sup> is taken as 0.162 nm in our calculation which is 0.034 nm smaller than the sum of radii  $r_{O^{2-}}$  (=0.132 nm) and  $r_{Fe^{3+}}$  (=0.064 nm). Moreover, Donnerberg et al. [47] obtained correct  $D$  value using superposition model with Fe<sup>3+</sup>–O<sup>2-</sup> distance about 0.15 nm in Fe<sup>3+</sup>:KTaO<sub>3</sub> system.

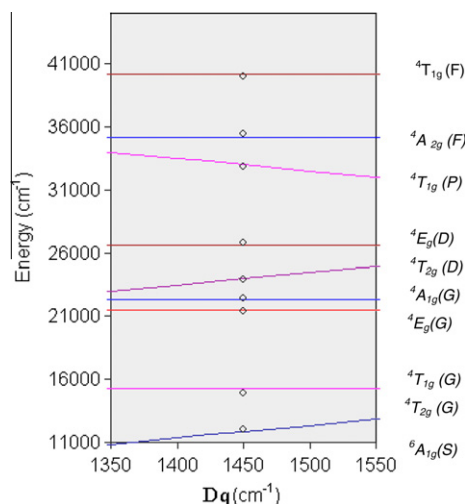


**Fig. 4.** Optical absorption spectrum of  $\text{Fe}^{3+}:\text{SN}$  at room temperature in the wavelength range (a) 195–325 nm and (b) 325–925 nm.

The crystal-field parameters  $B_{kq}$  using Eq. (6) are given [31] in Appendix C. The calculated  $B_{kq}$  parameters are obtained (in  $\text{cm}^{-1}$ ):  $B_{20} = -224.837$ ,  $B_{22} = -3215.4$ ,  $B_{40} = 0.043$ ,  $B_{42} = 0.835$  and  $B_{44} = -1.753$ . Using Eqs. (3) and (4) these values of  $B_{kq}$  yield the ZFS parameters given in Table 1. The  $|D|$  and  $|E|$  values thus obtained are in good agreement with the experimental one.

## 7. Conclusions

EPR study of  $\text{Fe}^{3+}$  ion doped SN single crystal has been done at 77 K. The spin Hamiltonian parameters ( $g$ ,  $|D|$ ,  $|E|$  and  $a$ ) have been



**Fig. 5.** The energy level diagram of  $\text{Fe}^{3+}:\text{SN}$  showing the variation of the levels with  $Dq$  for  $B = 934$  and  $C = 2059 \text{ cm}^{-1}$  (experimental energy values are shown by the circles).

**Table 3**

Observed and calculated energies of the absorption spectrum of  $\text{Fe}^{3+}:\text{SN}$ ;  $Dq = 1450$ ,  $B = 934$  and  $C = 2059 \text{ cm}^{-1}$ ; uncertainties are given in brackets.

Transition from	Observed wave number ( $\text{cm}^{-1}$ )	Calculated wave number ( $\text{cm}^{-1}$ )
${}^6A_{1g}(S)$		
${}^4T_{1g}(G)$	11650 (15)	11827
	12024 (18)	
	13793 (12)	
${}^4T_{2g}(G)$	14888 (15)	15283
	16173 (19)	
	17839 (18)	
	18576 (15)	
	19544 (20)	
${}^4E_g(G)$	21403 (14)	21483
${}^4A_{1g}(G)$	22472 (14)	22369
${}^4T_{2g}(D)$	23904 (20)	23972
${}^4E_g(D)$	26746 (22)	26590
${}^4T_{1g}(P)$	32796 (15)	32976
${}^4A_{2g}(F)$	35455 (12)	35108
${}^4T_{1g}(F)$	37412 (18)	
	39948 (14)	40170
	40789 (20)	

determined. The results indicate that  $\text{Fe}^{3+}$  ions enter the lattice substitutionally by replacing  $\text{Sr}^{2+}$  sites and the charge compensation in the crystal is effected either by excess oxygen ion or by vacancies distributed at random throughout the crystal. The optical absorption study has been carried out at room temperature and the observed bands have been assigned to transitions from the  ${}^6A_{1g}(S)$  ground state to the various excited states of  $\text{Fe}^{3+}$  ion in cubic crystal field approximation. The Racah parameters ( $B$ ,  $C$ ) and crystal field parameter ( $Dq$ ) have also been evaluated. The considerable decrease in the value of the parameters  $B$  and  $C$  (from 1130 to 934 and 4111 to 2059  $\text{cm}^{-1}$ ) shows that there exists a strong covalent bonding between the central metal ion and the ligands. Theoretical investigation of ZFS parameters have also been performed using perturbation formulae and crystal field parameters obtained using superposition model. There is good agreement between the theoretical and experimental results.

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## Appendix A

The allowed transitions and the fields  $B$  at which they occur when the Zeeman interaction is dominant as compared with the ZFS terms are given by [11,20]

$$M = +5/2 \leftrightarrow +3/2,$$

$$B = B_0 - 2D(3\cos^2\theta - 1) - (32D^2/B_0)\cos^2\theta\sin^2\theta + (D^2/B_0)\sin^4\theta - 2pa; \quad (\text{A.1})$$

$$M = +3/2 \rightarrow +1/2,$$

$$B = B_0 - D(3\cos^2\theta - 1) + (4D^2/B_0)\cos^2\theta\sin^2\theta - (5D^2/4B_0)\sin^4\theta + (5/2)pa; \quad (\text{A.2})$$

$$M = +1/2 \leftrightarrow -1/2,$$

$$B = B_0 + (16D^2/B_0)\cos^2\theta\sin^2\theta - (2D^2/B_0)\sin^4\theta; \quad (\text{A.3})$$

$$M = -1/2 \leftrightarrow -3/2,$$

$$B = B_0 + D(3\cos^2\theta - 1) + (4D^2/B_0)\cos^2\theta\sin^2\theta - (5D^2/4B_0)\sin^4\theta - (5/2)pa; \quad (\text{A.4})$$

$$M = -3/2 \leftrightarrow -5/2,$$

$$B = B_0 + 2D(3\cos^2\theta - 1) - (32D^2/B_0)\cos^2\theta\sin^2\theta + (D^2/B_0)\sin^4\theta + 2pa. \quad (\text{A.5})$$

where  $B_0 = hv/g\mu_B$  and  $\theta$  is the angle of rotation. The parameter  $p$  due to the cubic field is given by the expression  $p = (1-5\phi)$ , where  $\phi = (l^2m^2 + m^2n^2 + n^2l^2)$ ;  $(l, m, n)$  being the direction cosines of magnetic field with respect to the axes  $(x, y, z)$ .

## Appendix B

The electrostatic parameters  $B$  and  $C$  are calculated from the energy states  ${}^4E_g(G)$  and  ${}^4E_g(D)$  which are independent of  $Dq$  using the energy matrix [29]

The solution for the above equation is

$$T_1 = 1/2[(27B + 10C + 26\alpha) - \sqrt{49B^2 - 188B\alpha + 196\alpha^2}]$$

$$T_2 = 1/2[(27B + 10C + 26\alpha) + \sqrt{49B^2 - 188B\alpha + 196\alpha^2}]$$

$$(T_2 - T_1)^2 = [49B^2 - 188B\alpha + 196\alpha^2]$$

$$B = (94\alpha \pm \sqrt{49(T_2 - T_1)^2 - 768\alpha^2})/49$$

In the above expression we always take the positive value of  $\sqrt{49(T_2 - T_1)^2 - 768\alpha^2}$ .

$$B = (94\alpha + \sqrt{49(T_2 - T_1)^2 - 768\alpha^2})/49 \quad (\text{B.1})$$

Assuming  $188 \approx 196$ , we have

$$T = 1/2[(27B + 10C + 26\alpha) \pm (7B - 14\alpha)]$$

$$T_1 = 10B + 5C + 20\alpha = {}^4E_g(G)$$

$$T_2 = 17B + 5C + 6\alpha = {}^4E_g(D)$$

Thus,

$$C = (T_1 + T_2 - 27B - 26\alpha)/10 \quad (\text{B.2})$$

As the energy state  ${}^4E_g(G)$  lies lower than  ${}^4A_{1g}(G)$ ; we have taken  $T_1$  as  ${}^6A_{1g}(S) \rightarrow {}^4E_g(G)$  and  $T_2$  as  ${}^6A_{1g}(S) \rightarrow {}^4E_g(D)$ .

## Appendix C

Relations for the crystal-field parameters derived within the superposition model for the  $\text{Fe}^{3+}$  ion positioned at the  $\text{Sr}^{2+}$  site in SN:

$$B_{20} = \bar{A}_2(R_0) \left[ (R_0/R_1)^{t_2} (3\cos^2\theta_1 - 1) + (R_0/R_1')^{t_2} (3\cos^2\theta_1' - 1) + (R_0/R_2)^{t_2} (3\cos^2\theta_2 - 1) + (R_0/R_2')^{t_2} (3\cos^2\theta_2' - 1) \right] \quad (\text{C.1})$$

$$B_{22} = \sqrt{6}\bar{A}_2(R_0) \left[ (R_0/R_1)^{t_2} \sin^2\theta_1 \cos(2\phi_1) + (R_0/R_1')^{t_2} \sin^2\theta_1' \cos(2\phi_1') + (R_0/R_2)^{t_2} \sin^2\theta_2 \cos(2\phi_2) + (R_0/R_2')^{t_2} \sin^2\theta_2' \cos(2\phi_2') \right] / 2 \quad (\text{C.2})$$

$$B_{40} = \bar{A}_4(R_0) \left[ (R_0/R_1)^{t_4} (35\cos^4\theta_1 - 30\cos^2\theta_1 + 3) + (R_0/R_1')^{t_4} (35\cos^4\theta_1' - 30\cos^2\theta_1' + 3) + (R_0/R_2)^{t_4} (35\cos^4\theta_2 - 30\cos^2\theta_2 + 3) + (R_0/R_2')^{t_4} (35\cos^4\theta_2' - 30\cos^2\theta_2' + 3) \right] \quad (\text{C.3})$$

$$B_{42} = \sqrt{10}\bar{A}_4(R_0) \left[ (R_0/R_1)^{t_4} \sin^2\theta_1 (7\cos^2\theta_1 - 1) \cos(2\phi_1) + (R_0/R_1')^{t_4} \sin^2\theta_1' (7\cos^2\theta_1' - 1) \cos(2\phi_1') + (R_0/R_2)^{t_4} \sin^2\theta_2 (7\cos^2\theta_2 - 1) \cos(2\phi_2) + (R_0/R_2')^{t_4} \sin^2\theta_2' (7\cos^2\theta_2' - 1) \cos(2\phi_2') \right] \quad (\text{C.4})$$

$$B_{44} = \sqrt{70}\bar{A}_4(R_0) \left[ (R_0/R_1)^{t_4} \sin^4\theta_1 \cos(4\phi_1) + (R_0/R_1')^{t_4} \sin^4\theta_1' \cos(4\phi_1') + (R_0/R_2)^{t_4} \sin^4\theta_2 \cos(4\phi_2) + (R_0/R_2')^{t_4} \sin^4\theta_2' \cos(4\phi_2') \right] / 2 \quad (\text{C.5})$$

$$\begin{vmatrix} -22B + 5C + 12\alpha - E & -2\sqrt{3}B + 4\sqrt{3}\alpha \\ -2\sqrt{3}B + 4\sqrt{3}\alpha & -21B + 5C + 14\alpha - E \end{vmatrix} = 0$$

For the ground state  ${}^6A_{1g}(S)$ , the energy is  $-35B$ .

Substituting  $E = -35B + T$  in the above equation, we get

$$\begin{vmatrix} 13B + 5C + 12\alpha - T & (-2B + 4\alpha)\sqrt{3} \\ (-2B + 4\alpha)\sqrt{3} & 14B + 5C + 14\alpha - T \end{vmatrix} = 0$$

After solving the above matrix, we get

$$T = 1/2[(27B + 10C + 26\alpha) \pm \sqrt{49B^2 - 188B\alpha + 196\alpha^2}]$$

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